

## MATHEMATICS MAGAZINE

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$$\sum_{i=1}^N \left[ \left( \frac{x_i}{a_i} \right)^2 \right]^{n_i} = \text{Constant}$$

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